

$$(1) I_D = \frac{I_{DSS}}{2} = \frac{1.5 \text{ mA}}{2}$$

$$I_D = K(V_{GS} - V_T)^2$$

$$1.5 \text{ mA} = 2 \times 10^{-3} (V_{GS} - 2)^2$$

$$\therefore V_{GS} = 1.134 \text{ V}$$

$$V_{GS} = 2.866 \text{ V}$$

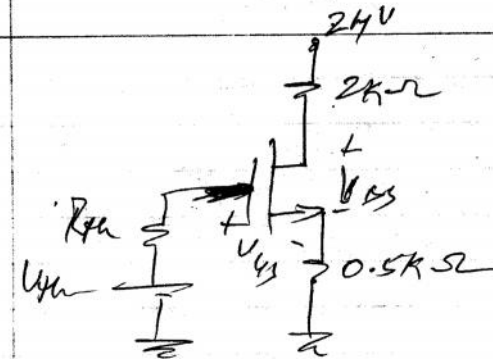
For V_{GS} to turn on $\Rightarrow V_{GS} > V_T$ $\therefore V_{GS} = 2.866 \text{ V}$

KVL to DS loop

$$24 - I_D(2\text{K}) - V_{DS} - I_D(0.5\text{K}) = 0$$

$$\text{in } I_D = I_D, V_{DS} = 20.25 \text{ V}$$

KVL to GS loop



$$V_{GS} - V_{GS} - I_D(0.5\text{K}) = 0$$

$$V_{GS} = 3.616 \text{ V}$$

Assuming $R_{th} = 1 \text{ M}\Omega$

$$V_{GS} = \frac{R_2(24)}{R_1 + R_2}$$

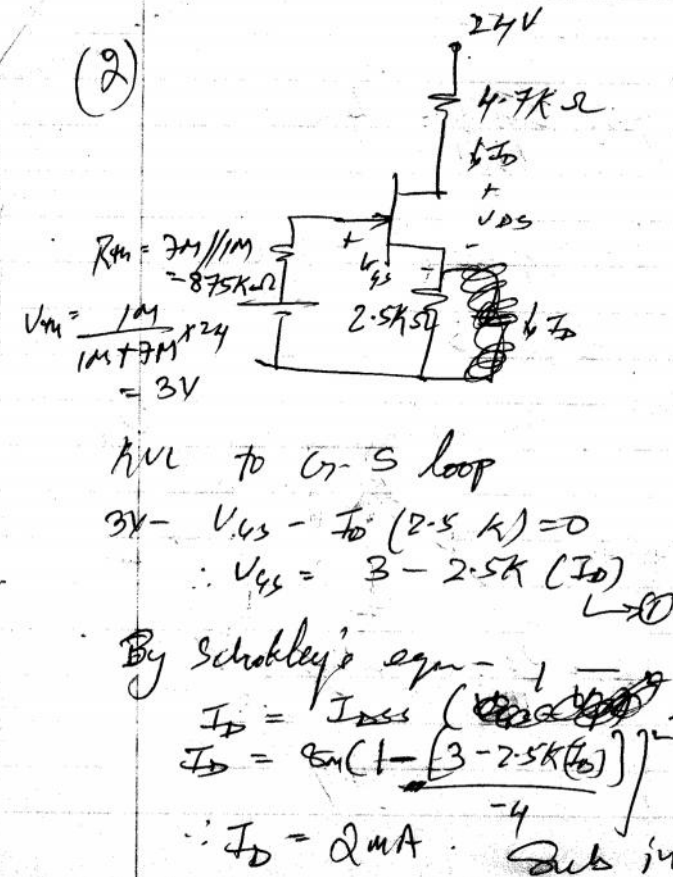
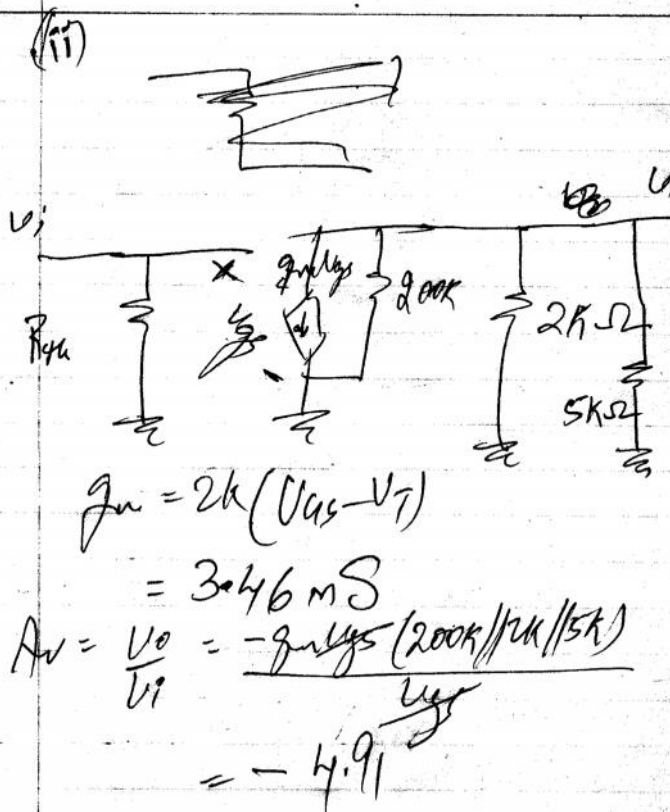
$$R_{th} = \frac{R_1 R_2}{R_1 + R_2}$$

$$\therefore \frac{R_2}{R_1 + R_2} = 0.15$$

$$\therefore 1\text{M} = R_1(0.15)$$

$$\therefore R_1 = 6.62 \text{ M}\Omega$$

$$\therefore R_2 = 1.18 \text{ M}\Omega$$

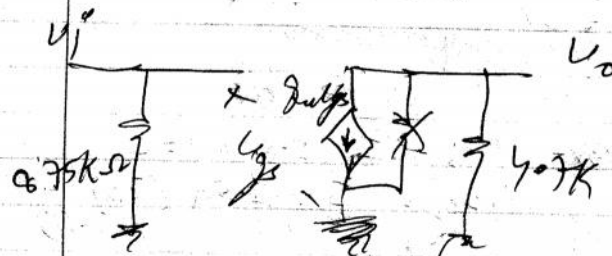


$$V_{GS} = -2V$$

$$g_{m0} = \frac{2I_{DSS}}{|V_p|} = 4mS$$

$$g_m = g_{m0} \left(1 - \frac{V_{GS}}{V_p}\right)$$

$$= 2mS$$



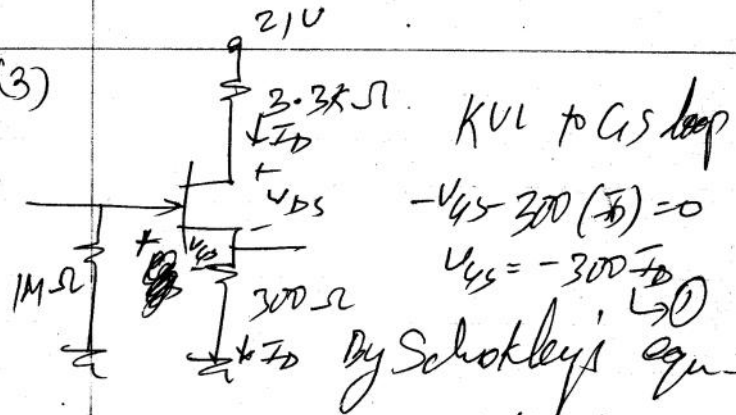
$$A_v = \frac{v_o}{v_i} = -g_m R_D$$

$$= -9.4$$

$$R_i = 8.75k\Omega$$

$$R_o = 4.7k\Omega$$

(3)



$$I_D = 8\text{mA} \left(1 - \frac{-300I_D}{-4}\right)^2$$

$$\therefore I_D = 3.96\text{mA}$$

sub in ①

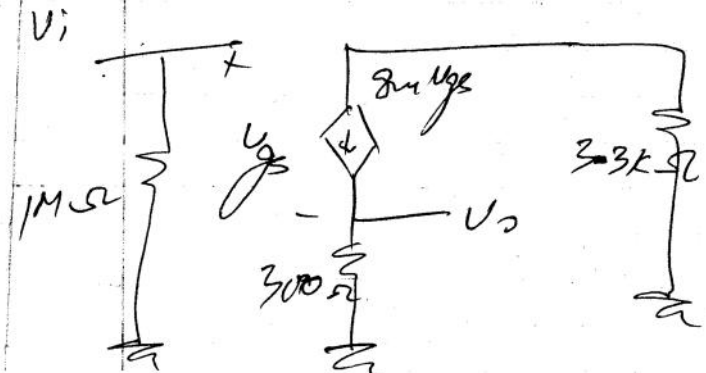
$$V_{GS} = -1.19\text{V}$$

$$g_{m0} = \frac{2I_{DSS}}{|V_p|} = 4\text{mS}$$

$$g_m = g_{m0} \left(1 - \frac{V_{GS}}{V_p}\right)$$

$$= 4\text{mS} \left(1 - \frac{-1.19}{4}\right)$$

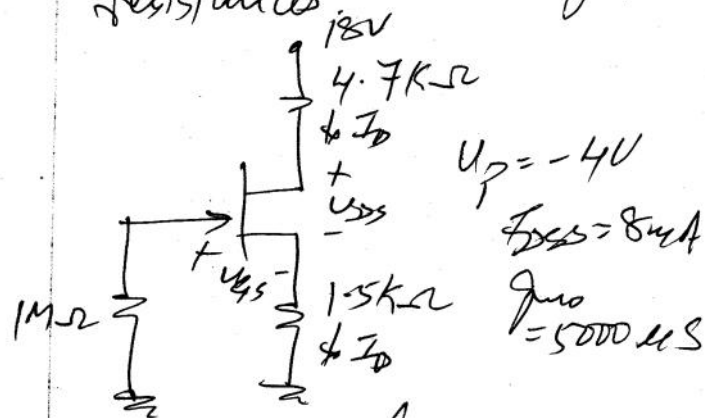
$$= 2.81\text{mS}$$



$$A_v = \frac{V_o}{V_i} = \frac{300(g_m V_{gs})}{V_{gs} + g_m V_{gs}(300)} = 0.457$$

$$R_i = 1\text{M}\Omega \quad R_o = 300\Omega \parallel \frac{1}{g_m} = 162.78\Omega$$

4) Type of biasing : Self bias
with source degeneration
resistances



KVL to GS loop,
 $-V_{GS} - 1.5K I_D = 0$
 $V_{GS} = -1.5K I_D$ — (1)
 By Shockley's eqn

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

$$\therefore I_D = 8mA \left(1 - \frac{-1.5K I_D}{-4}\right)^2$$

$$\therefore I_D = 1.51mA$$

Sub in (1)

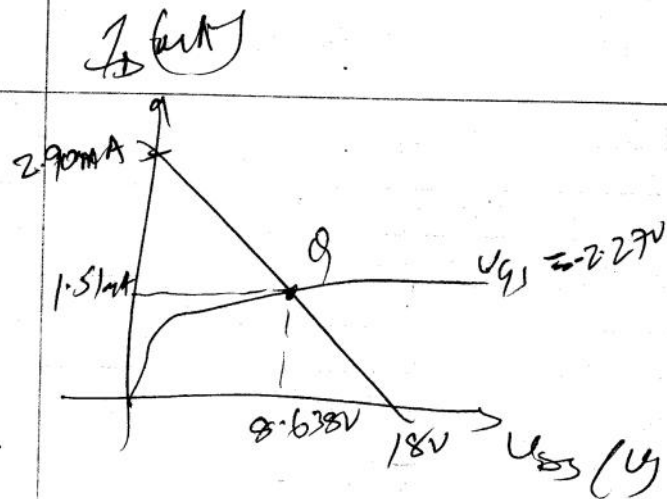
$$V_{GS} = -2.27V$$

KVL to DS loop.

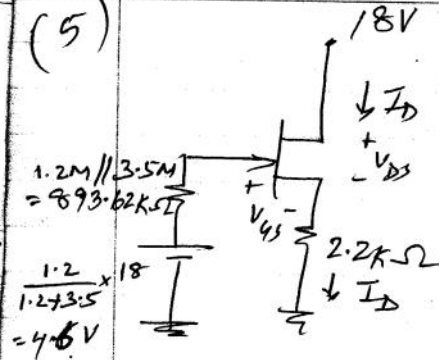
$$18 - 4.7K I_D - 1.5K I_D - V_{DS} = 0$$

$$\therefore V_{DS} = 8.638V$$

$$Q = (8.638V, 1.5mA)$$



(5)



Applying KVL to G-S loop

$$4.6 - V_{GS} - 2.2K(I_D) = 0$$

$$V_{GS} = 4.6 - 2.2K(I_D) \quad \text{--- (1)}$$

By Shockley's eqn

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

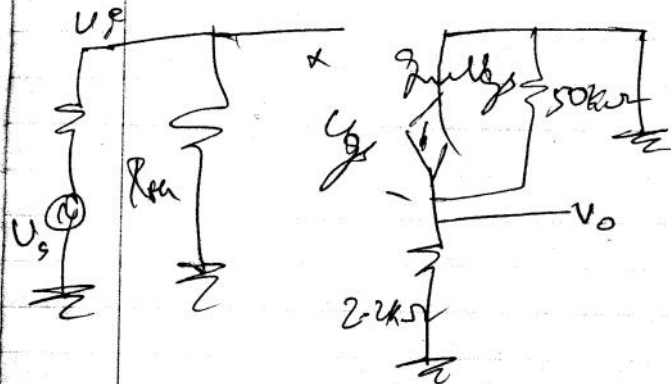
$$I_D = 7mA \left(1 - \frac{4.6 - 2.2K(I_D)}{-4}\right)^2$$

$$\therefore I_D = 2.77mA$$

αυτ in ①
 $V_{as} = -1.49V$

$g_{m0} = 5000 \mu S$

$g_m = g_{m0} \left(1 - \frac{V_{as}}{V_p}\right)$
 $= 3.14 \mu S$



$\mu = \frac{V_o}{V_i} = \frac{g_m \cdot 2.2k \parallel 50k}{g_m \parallel 2.2k \parallel 50k}$

$= \cancel{0.87} 0.87$

$R_i = 893.6k\Omega$

$R_o = 50k \parallel 2.2k \parallel 1/g_m$
 $= 276.66\Omega$

②

①

$$I_{D_{on}} = K(V_{GS_{on}} - V_T)^2$$

$$200 \mu A = K(2 - V_T)^2$$

$$K = 50 \mu A/V^2$$

$$I_{D_{on}} = 2K(V_{GS} - V_T)^2$$

$$23 \mu A = 2 \times 50 (V_{GS} - 2)^2$$

$$\therefore V_{GS} = 2.23V$$

$$g_m = 2\sqrt{K_n I_D}$$

$$\therefore I_D = 2.645 \mu A$$

~~Apply to DS loop~~
 ~~$24 = 3.3K I_D + V_{DS}$~~

KVL to GS loop

$$V_{GS} - V_{GS} - I_D R_S = 0$$

$$8.2K \times 2.23 - 2.23 - (2.645 \mu A) R_S = 0$$

$$8.2K + 47K$$

$$\therefore R_S = 504.81 \Omega$$

KVL to DS loop-

$$24 - I_D(3.3K) - V_{DS} - (2.645 \mu A)(R_S) = 0$$

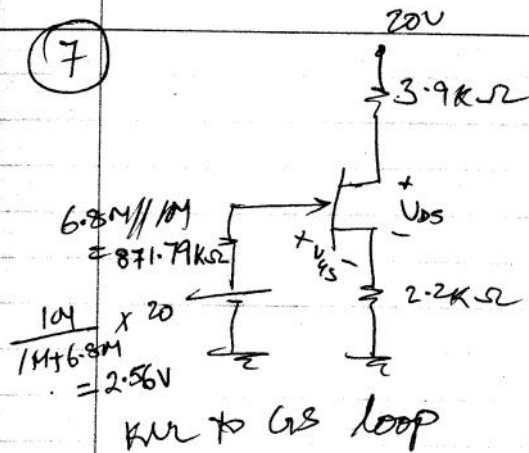
$$g_m = 23 \mu S \quad \therefore V_{DS} = 13.94V$$

$$A_v = \frac{V_o}{V_i} = \frac{-g_m V_{GS}(3.3K)}{V_{GS}}$$

$$\frac{V_o}{25mV} = -37.95$$

$$\therefore V_o = -0.95V$$

(7)



$$2.56 - V_{GS} - I_D(2.2k) = 0$$

$$V_{GS} = 2.56 - 2.2k(I_D)$$

By Shockley's eqn

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

$$I_D = 10mA \left(1 - \frac{2.56 - 2.2kI_D}{-4V}\right)^2$$

$$\therefore I_D = 2.24mA$$

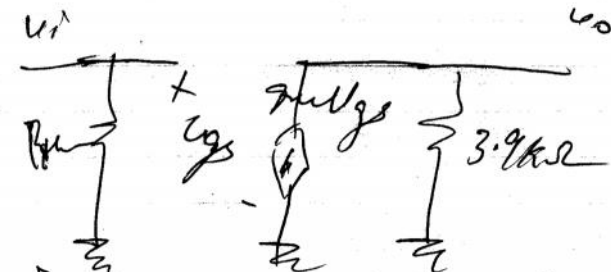
Sub in ①

$$V_{GS} = -2.37V$$

$$g_{m0} = \frac{2I_{DSS}}{V_P} = 4.44mA/V$$

$$g_m = g_{m0} \left(1 - \frac{V_{GS}}{V_P}\right)$$

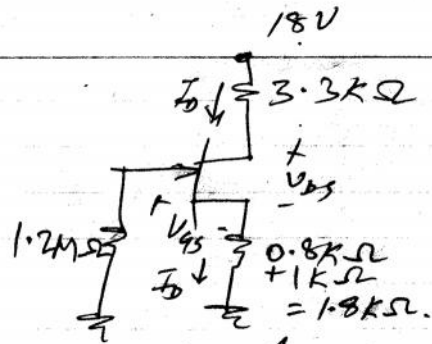
$$= 2.10mA/V$$



$$R_1 = R_{th} = 871.79k\Omega \quad R_D = 3.9k\Omega$$

$$A_{v_o} = \frac{v_o}{u_i} = \frac{-g_m R_D}{1 + g_m R_D} = 8.19$$

(8)



KVL to GS loop

$$-V_{GS} = I_D(1.8k\Omega) = 0$$

$$\therefore V_{GS} = -I_D(1.8k\Omega) \quad \text{--- (1)}$$

By Shockley's eqn.

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

$$I_D = 8mA \left(1 - \frac{-1.8kI_D}{-4}\right)^2$$

$$I_D = 1.32mA$$

sub in (1)

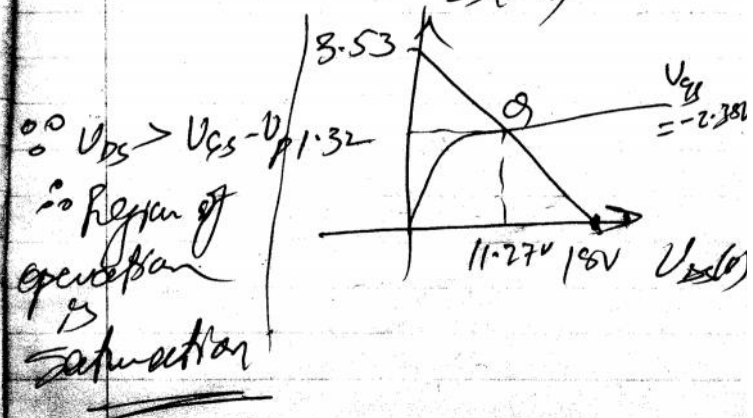
$$V_{GS} = -2.38V$$

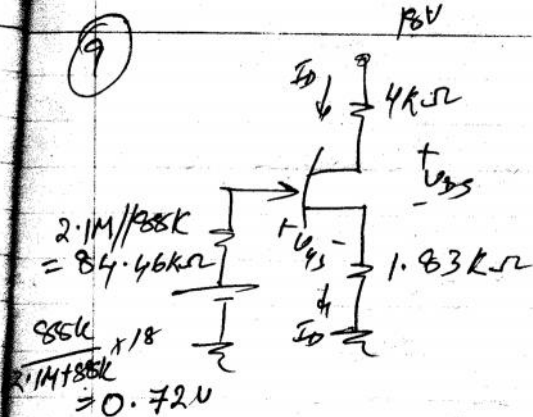
KVL to DS loop

$$18 - 3.3k(I_D) - V_{DS} - 1.8kI_D = 0$$

$$V_{DS} = 11.27V$$

$$Q = (11.27V, 1.32mA)$$





KVL to GS loop

$$0.72 - V_{GS} - 1.83K(I_D) = 0$$

$$V_{GS} = 0.72 - 1.83K I_D \quad \text{--- ①}$$

By Shockey's eqn

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_{th}}\right)^2$$

$$I_D = 8mA \left(1 - \frac{0.72 - 1.83K I_D}{4}\right)^2$$

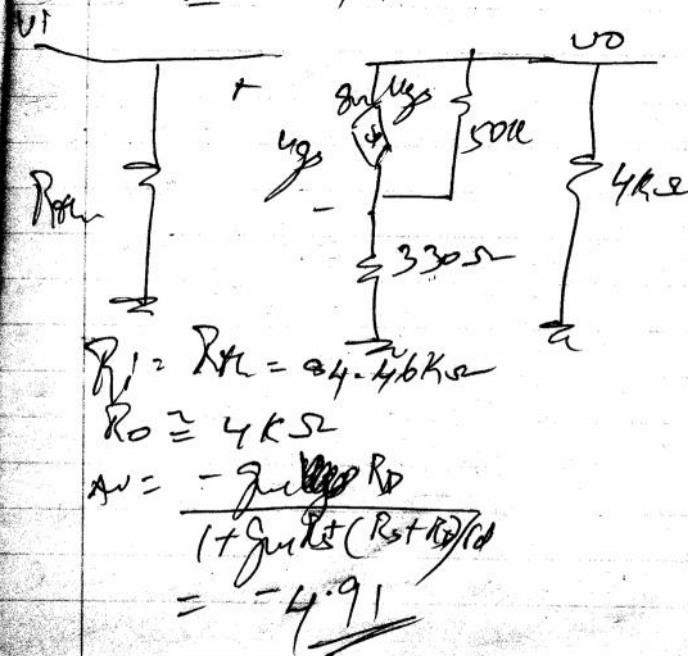
$$\therefore I_D = 1.6mA$$

Sub in ① $V_{GS} = -2.21V$

$$g_m = g_{m0} \left(1 - \frac{V_{GS}}{V_{th}}\right)$$

$$= 5000 \times 10^{-6} \left(1 - \frac{-2.21}{4}\right)$$

$$= 2.24 mS$$

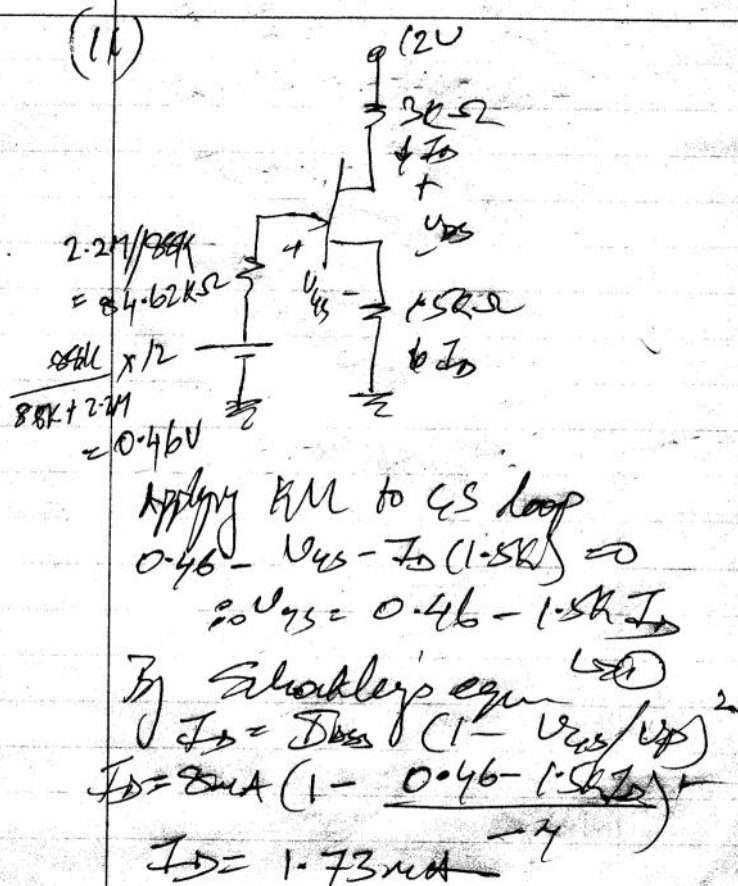


(10) $I_{DQ} = k_n (V_{GSQ} - V_{TN})^2$
 $200 = k_n (4 - 2)^2$
 $\therefore k_n = 50 \text{ mA/V}^2$

22V
 $I_D \downarrow$ 2.2kΩ
 V_{GS}
 V_{DS}
 $I_D \downarrow$ 330Ω
 V_{GS}
 V_{DS}
 I_D

51k/9.1k
 $7.74k\Omega$
 $4.1k\Omega$
 $3.33V$
 k_n to GS loop
 $3.33 - V_{GS} - 330 I_D = 0$
 $V_{GS} = 3.33 - 330 I_D$
 $I_D = 73 \mu A$

$I_D = k_n (V_{GS} - V_{TN})^2$
 $I_D = 50 \text{ mA/V}^2 (3.33 - 380 I_D - 2)^2$
 $I_D = 4.03 \text{ mA}$ 3.257mA
 $V_{GS} = 2.255V$
 KVL to DS loop
 $22 - 2.2k I_D - V_{DS} - 330 I_D = 0$
 $\therefore V_{DS} = 11.8V$ 13.76V
 $V_D = 22 - 2.2k (I_D)$
 $= 13.13V$ 14.835V



* KVL to DS loop

$$12 - 30k\Omega(I_D) - V_{DS} - 1.5k\Omega I_D = 0$$

$$V_{DS} = 4.22V \quad Q = (4.22V, 1.72mA)$$

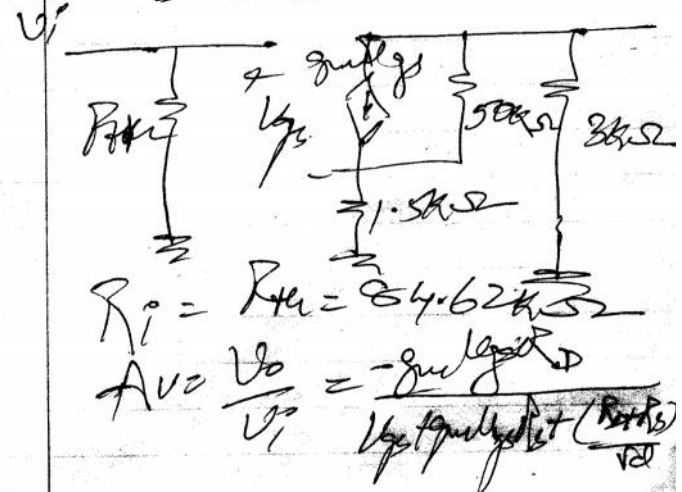
Calculation ①

$$V_{GS} = -2.14V$$

$$g_{mi} = g_{mo} \left(1 - \frac{V_{GS}}{V_{GS(0)}}\right)$$

$$= 5000 \times 10^{-6} \left(1 - \frac{-2.14}{4}\right)$$

$$= 2.33mS \quad V_O$$



$$V = -1.52$$

$$R_p = 84.62 \text{ k}\Omega$$

(12) (i) No reason why V_{GS} & I_{DQ} are given. If they were not given then we ~~had~~ get $I_{DQ} = 1.39 \text{ mA}$ & $V_{GS} = +5.41 \text{ V}$. Assuming its not room temp.

∴ Taking what is given

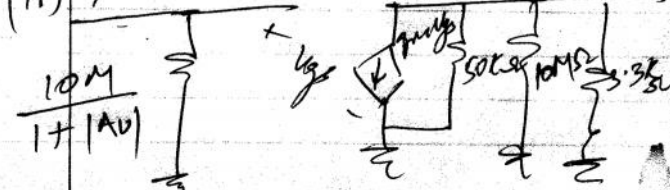
$$g_m = 2K(V_{GS} - V_T)$$

$$= 2 \times 0.24 \text{ mA} (6.4 - 3)$$

$$= 1.63 \text{ mS}$$

$$r_d = 1/y_{os} = 50,000 \Omega$$

(ii) V_i



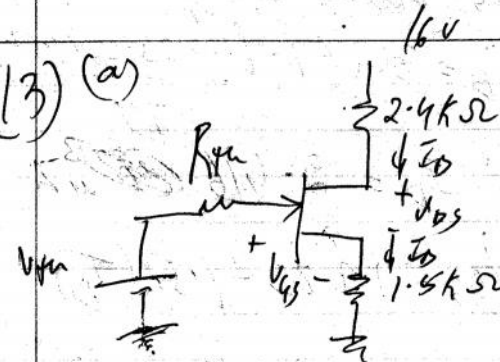
$$A_v = \frac{V_o}{V_i} = - \beta \mu_{V_{gs}} \left(\frac{50k \parallel 10M \parallel 3.3k}{V_{gs}} \right)$$

$$A_v = -5.04$$

$$Z_i = \frac{10M}{1 + |A_v|} = 1.66 M\Omega$$

$$Z_o = 3.09 k\Omega$$

(13) (a)



$$V_{gs} = \frac{2.4k\Omega}{2.4k\Omega + 2.1M\Omega} \times 16$$

$$= 1.823V$$

$$R_{th} = 2.1M \parallel 2.4k = 239.241 k\Omega$$

(i) KVL to G-S loop

$$1.823 - V_{gs} - I_D (1.5k) = 0$$

$$\therefore V_{gs} = 1.823 - I_D (1.5k\Omega)$$

By Shockley's eqn 2

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$$

$$I_D = 8 \text{ mA} \left(1 - \frac{1.823 - I_D(1.5 \text{ k})}{-4} \right)^2$$

$$\therefore I_D = 2.416 \text{ mA}$$

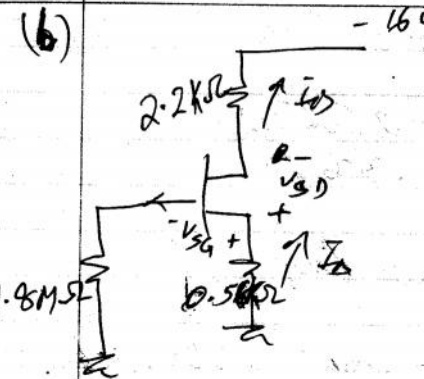
$$V_{GS} = 1.823 + 1.5 \text{ k}(I_D)$$

$$= -1.801 \text{ V}$$

KVL to DS loop

$$16 - 2.4 \text{ k} I_D - V_{DS} - 1.5 \text{ k} I_D = 0$$

$$\therefore V_{DS} = 6.578 \text{ V}$$



KVL to G-S loop

$$-I_D(0.56 \text{ k}) - V_{GS} = 0$$

$$V_{GS} = (-0.56 \text{ k}) I_D$$

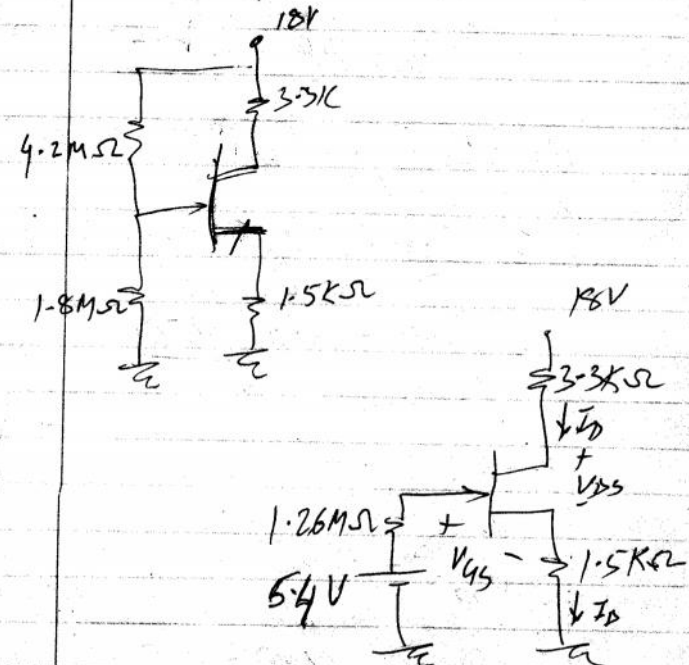
By Shockley's Eqn -

$$I_D = I_{DSS} \left(1 + \frac{V_{GS}}{V_P} \right)^2$$

$$I_D = 9 \text{ mA} \left(1 - \frac{0.56 \text{ k} I_D}{4.5} \right)^2$$

$$\begin{aligned}
 \therefore I_D &= 3.225 \text{ mA} \\
 \therefore V_{GS} &= -0.56k I_D \\
 &= -1.806 \text{ V} \\
 \text{KVL to } 2S \text{ loop} \\
 -0.56k I_D + V_{GS} - 2.2k I_D + 26 &= 0 \\
 \therefore \underline{V_{GS} = -7.099 \text{ V}}
 \end{aligned}$$

(14) BJT used Voltage divider with sawtooth source resistance.



KVL to GS loop

$$5.4 - V_{GS} - 1.5K(I_D) = 0$$

$$\therefore V_{GS} = 5.4 - 1.5K(I_D) \quad \text{--- (1)}$$

By Shockley's Eqn -

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

$$I_D = 8mA \left(1 - \frac{(5.4 - 1.5K I_D)}{-4}\right)^2$$

$$\therefore I_D = 4.31mA$$

Sub in (1)

$$V_{GS} = -1.065V$$

KVL to DS loop -

$$18 - 3.3K(I_D) - V_{DS} - 1.5K(I_D) = 0$$

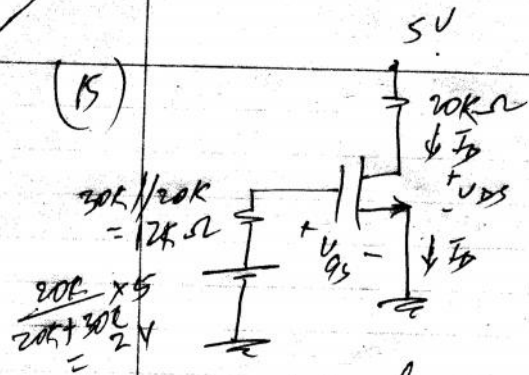
$$\therefore V_{DS} = -2.688V$$

$\because V_{DS} \neq V_{GS} - V_T$ $\therefore$ Not saturation

$V_{DS} < 0$ $\therefore$ In cut-off region.

$$Q = (-2.688V, 4.31mA)$$

(15)



KVL to GS loop

$$V_{gs} = 2V$$

$$I_D = k_n (V_{gs} - V_t)^2 = 0.1mA$$

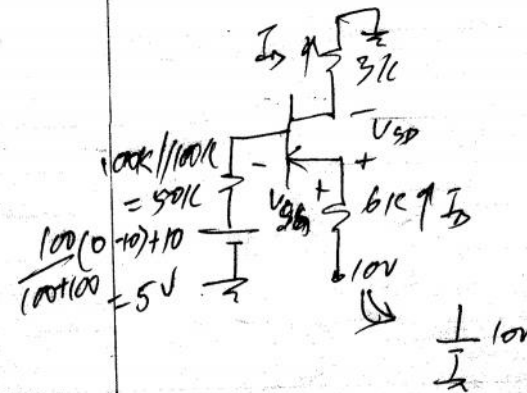
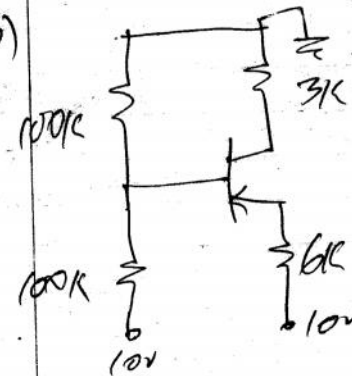
KVL to DS loop

$$5 - V_{ds} - 20k I_D = 0$$

$$V_{ds} = 3V \quad Q(3V, 0.1mA)$$

$\therefore V_{ds} > V_{gs} - V_t$
 so Region of operation is saturation

(16)

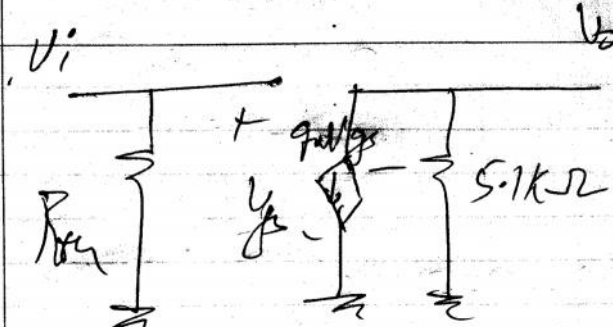


Ans in ①

$$V_{GS} = -1.84V$$

$$g_{m0} = \frac{2I_{DSS}}{V_{p1}} = 5.71mS$$

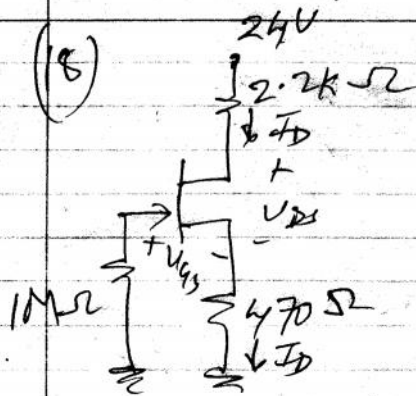
$$\begin{aligned} g_m &= g_{m0} \left(1 - \frac{V_{GS}}{V_p} \right) \\ &= 5.71m \left(1 - \frac{(-1.84)}{(-3.5)} \right) \\ &= \underline{\underline{2.71mS}} \end{aligned}$$



$$R_i = R_{Gi} = 1.02M\Omega$$

$$R_o = 5.1K\Omega$$

$$\begin{aligned} A_v &= \frac{V_o}{V_i} = \frac{g_m V_{GS} (5.1)K}{V_{GS}} \\ &= \underline{\underline{-13.82}} \end{aligned}$$



KVL to GS loop

$$-V_{GS} - 470 I_D = 0$$

$$V_{GS} = -470 I_D$$

By Shockley's eqn

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

$$I_D = 10mA \left(1 - \frac{-470 I_D}{-3.5}\right)^2$$

$$I_D = 3.22mA$$

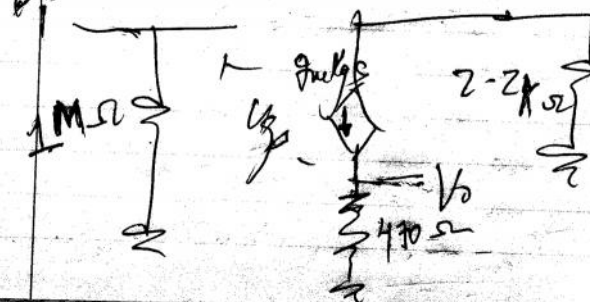
sub in ①

$$V_{GS} = -1.51V$$

$$g_{m0} = \frac{2I_{DSS}}{V_p} = 5.71mS$$

$$g_m = g_{m0} \left(1 - \frac{V_{GS}}{V_p}\right)$$

$$= 3.25mS$$



$$R_i = 104 \Omega$$

$$R_o = 200 \Omega$$

$$R_{eq} = 470 \Omega \parallel \frac{1}{g_m}$$

$$= 185.95 \Omega$$

$$A_v = \frac{v_o}{v_i} = \frac{g_m R_o (470)}{g_m + g_m R_o (470)}$$

$$= 0.604$$

$$(19) \quad I_D = 160 \mu A$$

$$I_D = K_n (V_{GS} - V_{TN})^2$$

$$\therefore V_{GS} = 2V$$

$$R_{eq} = \frac{V_{GS}}{I_D} = \frac{2V}{160 \mu A} = 12.5 k\Omega$$

$$R_{eq} = 12.5 k\Omega$$

$$V_{GS} = V_G - V_S$$

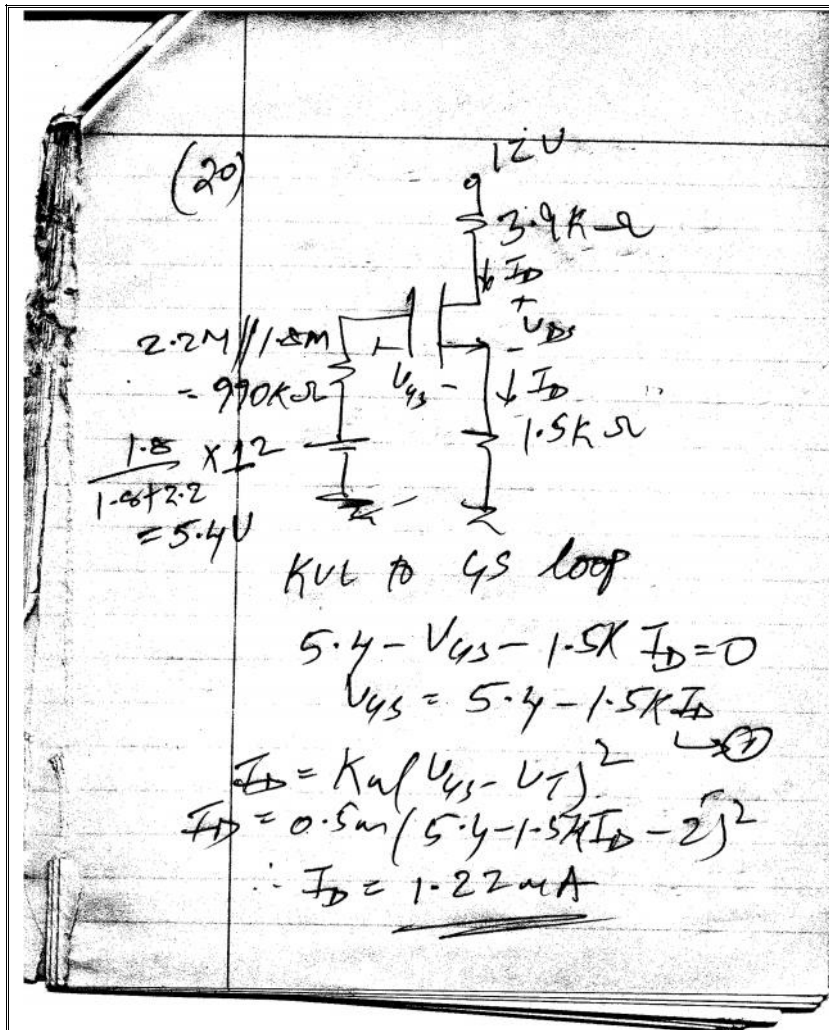
$$\text{But } V_G = 0$$

$$\therefore V_S = -2V$$

$$V_{DS} = V_D - V_S$$

$$\therefore V_D = 3 - 2 = 1V$$

$$I_D = \frac{5 - V_D}{R_D} \quad \therefore R_D = 25 k\Omega$$



πάλιν ①

$$V_{GS} = 3.57V$$

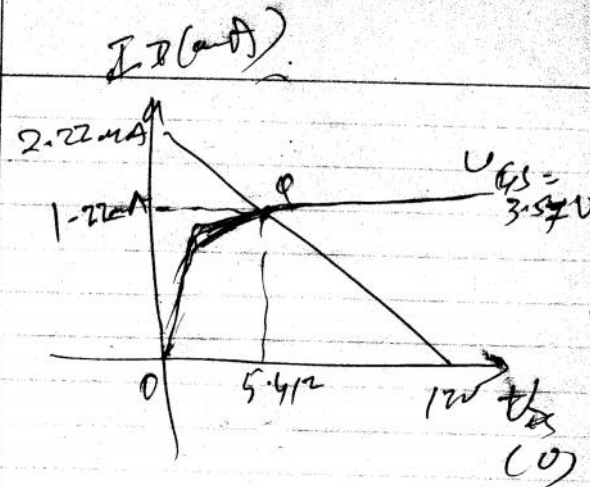
✗ KVL to DS loop

$$12 - 39K I_D - V_{DS} - 1.5K I_D = 0$$

$$\therefore V_{DS} = 5.412$$

$$\because V_{DS} > V_{GS} - V_T$$

$\therefore$ Region of operation
is saturation



$$Q = (5.412V, 1.22mA)$$