



Fig. 5-6

Now consider the tools we need to turn this basic idea into an efficient algorithm. For point  $(x, y)$  inside the clipping window, we have

$$x_{\min} \leq x_1 + \Delta x \cdot u \leq x_{\max}$$

$$y_{\min} \leq y_1 + \Delta y \cdot u \leq y_{\max}$$

Rewrite the four inequalities as

$$p_k u \leq q_k, \quad k = 1, 2, 3, 4$$

where

$$p_1 = -\Delta x \quad q_1 = x_1 - x_{\min} \quad (\text{left})$$

$$p_2 = \Delta x \quad q_2 = x_{\max} - x_1 \quad (\text{right})$$

$$p_3 = -\Delta y \quad q_3 = y_1 - y_{\min} \quad (\text{bottom})$$

$$p_4 = \Delta y \quad q_4 = y_{\max} - y_1 \quad (\text{top})$$

Observe the following facts:

- if  $p_k = 0$ , the line is parallel to the corresponding boundary and
  - if  $q_k < 0$ , the line is completely outside the boundary and can be eliminated
  - if  $q_k \geq 0$ , the line is inside the boundary and needs further consideration,
- if  $p_k < 0$ , the extended line proceeds from the outside to the inside of the corresponding boundary line,
- if  $p_k > 0$ , the extended line proceeds from the inside to the outside of the corresponding boundary line,
- when  $p_k \neq 0$ , the value of  $u$  that corresponds to the intersection point is  $q_k/p_k$ .

The Liang-Barsky algorithm for finding the visible portion of the line, if any, can be stated as a four-step process:

1. If  $p_k = 0$  and  $q_k < 0$  for any  $k$ , eliminate the line and stop. Otherwise proceed to the next step.
2. For all  $k$  such that  $p_k < 0$ , calculate  $r_k = q_k/p_k$ . Let  $u_1$  be the maximum of the set containing 0 and the calculated  $r$  values.
3. For all  $k$  such that  $p_k > 0$ , calculate  $r_k = q_k/p_k$ . Let  $u_2$  be the minimum of the set containing 1 and the calculated  $r$  values.
4. If  $u_1 > u_2$ , eliminate the line since it is completely outside the clipping window. Otherwise, use  $u_1$  and  $u_2$  to calculate the endpoints of the clipped line.